Statistics Mini-course Problem Set 1

Due on Thu. Mar 31

We will do some of the exercises in Hogg, Bovy, & Lang (HBL; 2010) (1008.4686), with some slight variations. You should solve these exercises on a computer and the best way to hand in the problem set is as an ipython notebook. Rather than sending me the notebook, you can upload it to GitHub, which will automatically render the notebook. Rather than starting a repository for a single notebook, you can upload your notebook as a gist, which are version-controlled snippets of code.

If you want to upload your notebook as a gist from the command-line, you can use the package at this http URL and use it as follows. Log into your GitHub account:

gist --login

and then upload your notebook statminicourse_2016_PS1_YOURNAME.ipynb as

gist statminicourse_2016_PS1_YOURNAME.ipynb

If you want to make further changes, you can clone your gist in a separate directory and use it as you would any other git repository.

Problem 1: Do exercise 1 in BHL.

Problem 2: Do exercise 1, but assuming that the errors σ_y of neighboring data points in x are correlated with a correlation coefficient of $\rho = 0.5$. E.g., data points 15 and 16 have y measurements whose uncertainty is described by a covariance matrix $\begin{pmatrix} \sigma_{y,15}^2 & 0.5 \sigma_{y,15} \sigma_{y,16} \\ 0.5 \sigma_{y,15} \sigma_{y,16} & \sigma_{y,16}^2 \end{pmatrix}$. Note that the data points in Table 1 are not sorted on x! How does the uncertainty variance σ_m^2 on the slope change?

Problem 3: Write a Metropolis-Hastings sampler for a general one-dimensional probability distribution p(x) with a Gaussian proposal distribution (characterized by a width parameter that should be passed to the code) that returns a sampling and the acceptance fraction. Test it with a Gaussian with zero mean and unit variance: plot a normalized histogram of the samples and compare it to the analytical PDF. Then apply it to sample a probability distribution consisting of the sum of two Gaussians with equal weights, unit variance for each, and means 0 and 10 (again plot a histogram of the samples and the analytical PDF). Try to find a relatively high acceptance fraction.

Problem 4: Solve exercise 6 in HBL using MCMC sampling with emcee.