### stellar systems

Large N systems interacting with long-range forces

 $F = G M m / r^2$ 

Examples of stellar systems:

globular cluster

galaxy

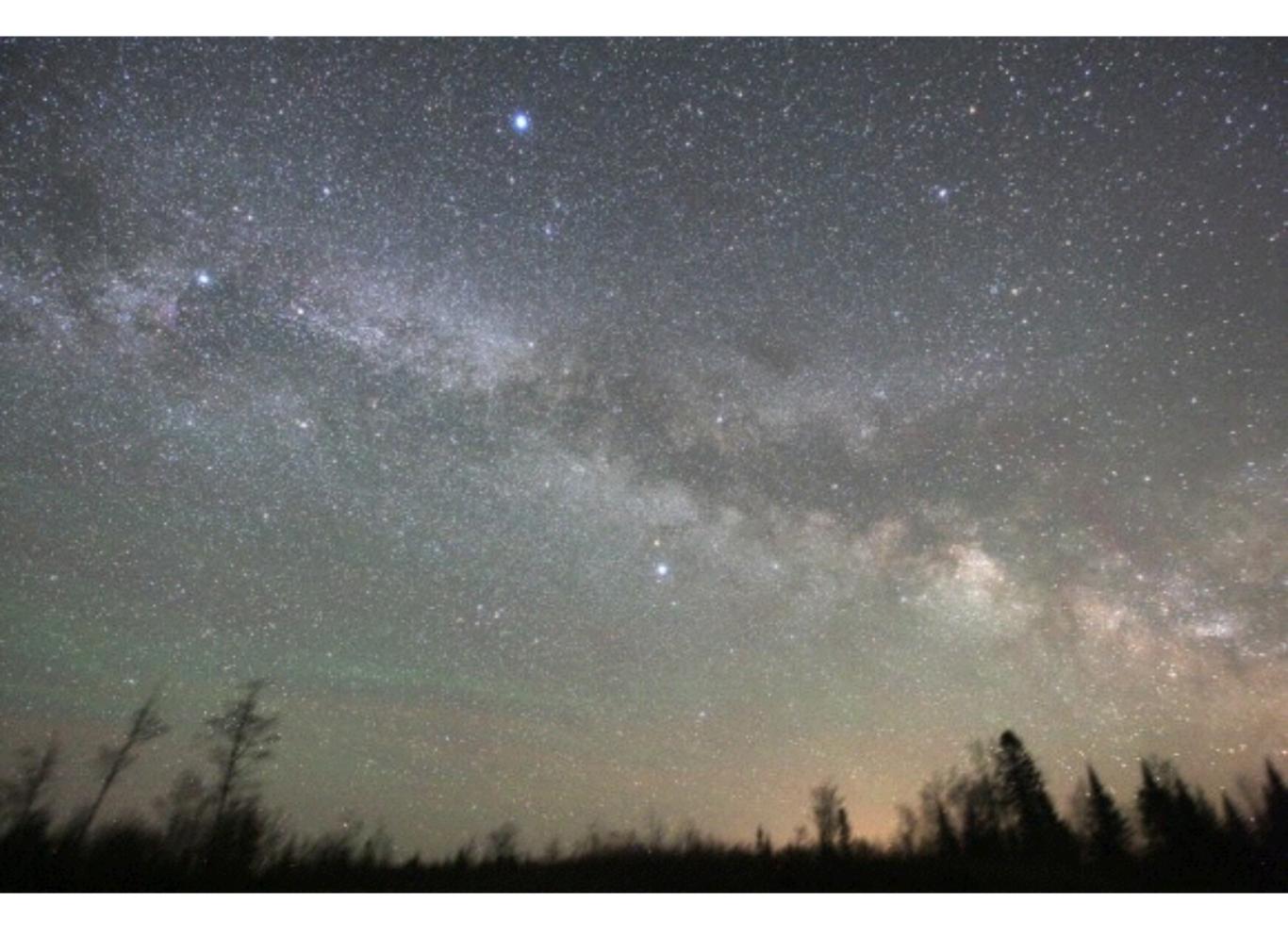
cluster of galaxy

connection to celestial mechanics, statistical mechanics, and plasma physics

# Overview of a typical galaxy (the Milky Way)

facts and puzzles

lecture hours: Friday 10-12?





# Effects of dust absorption & scattering

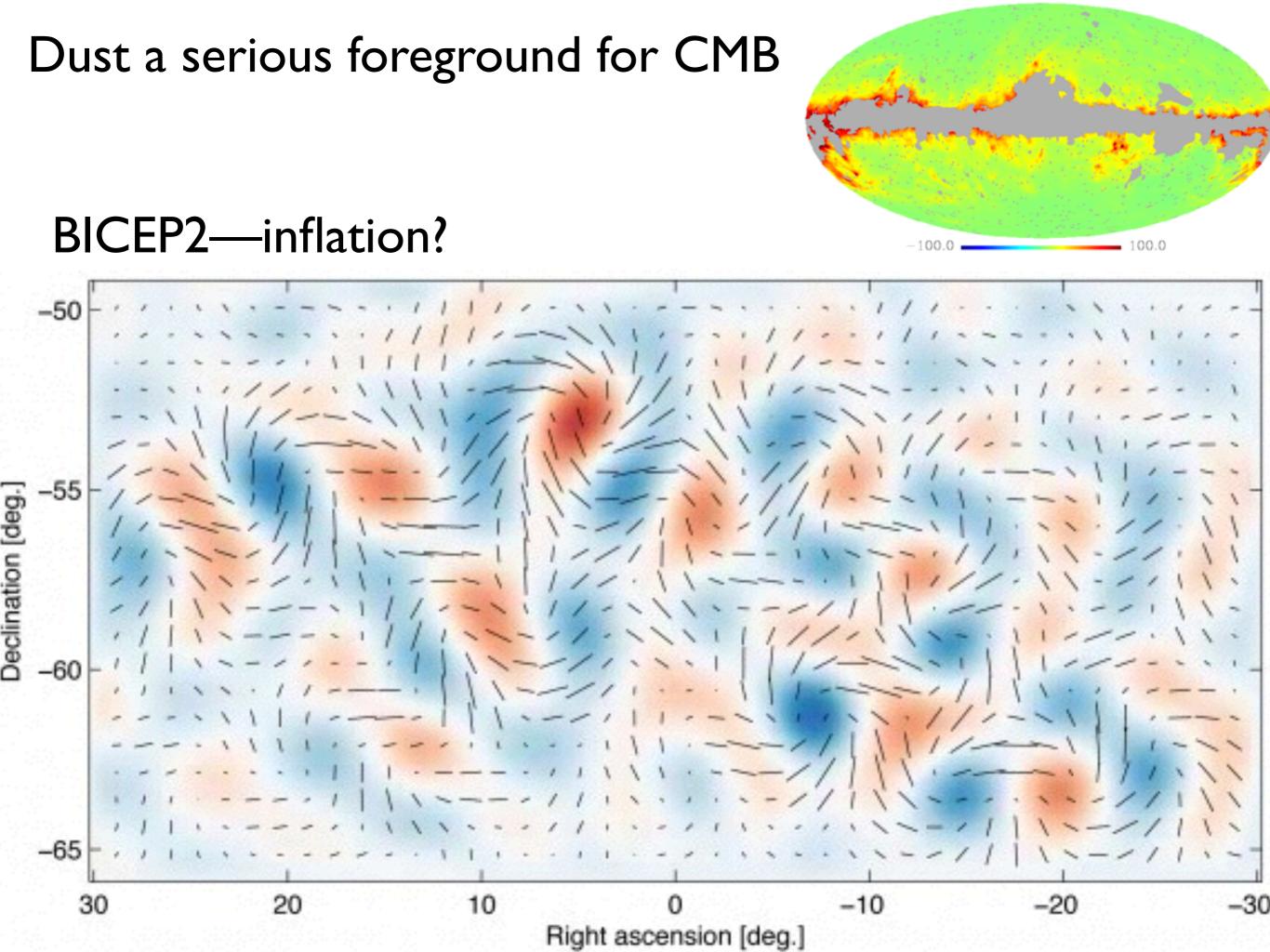
Interstellar Extinction  $A_x=(m-m_0)_x$   $A_B \sim 1.6 \text{ mag (d/kpc)}$  if  $n_H \sim 1/\text{cm}^3$ galactic center stars suffer A ~ 30 mag, or  $1/10^{12}$  photons pass through

Interstellar Reddening  $E(B-V)=A_B-A_v \sim 0.5 \text{ (d/kpc)}$ 

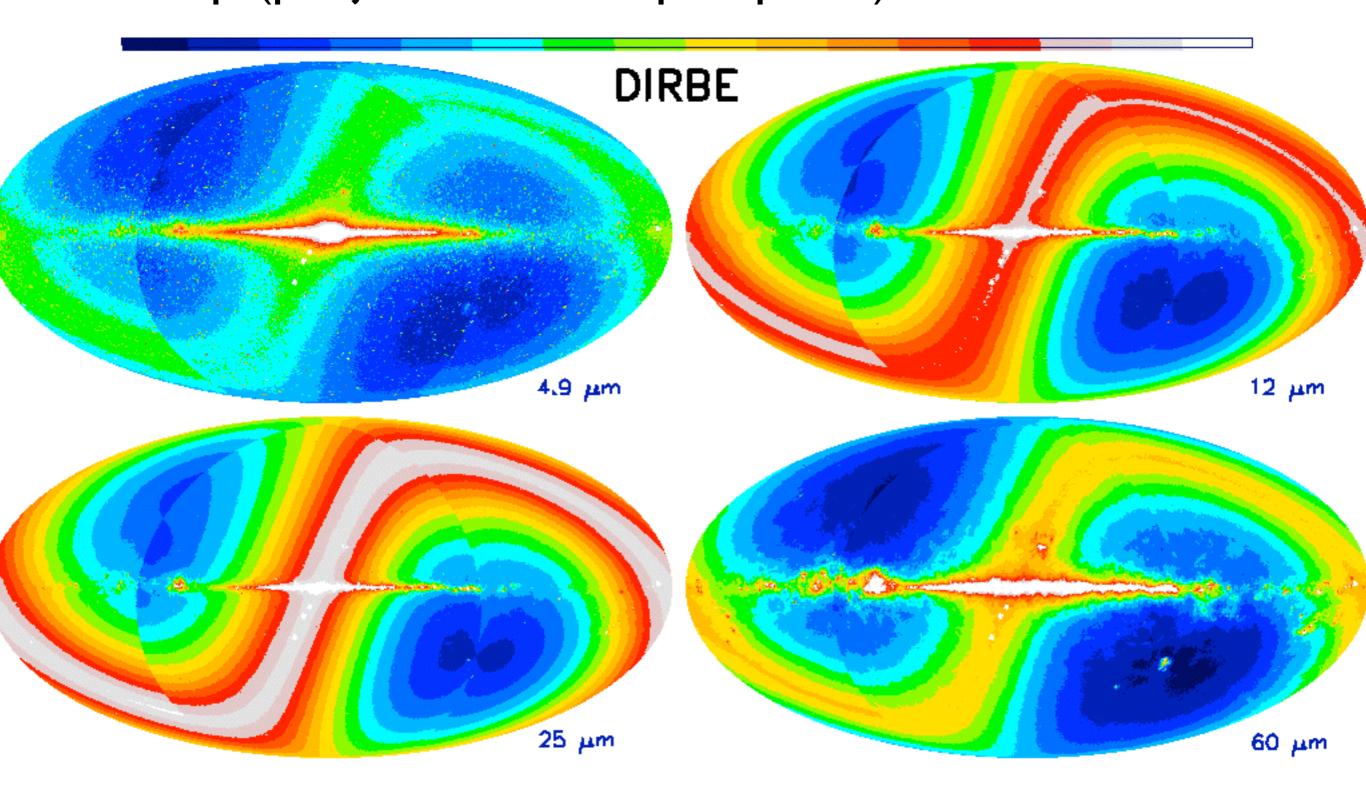
# DIRBE 1.25, 2.2, 3.5 μm Composite

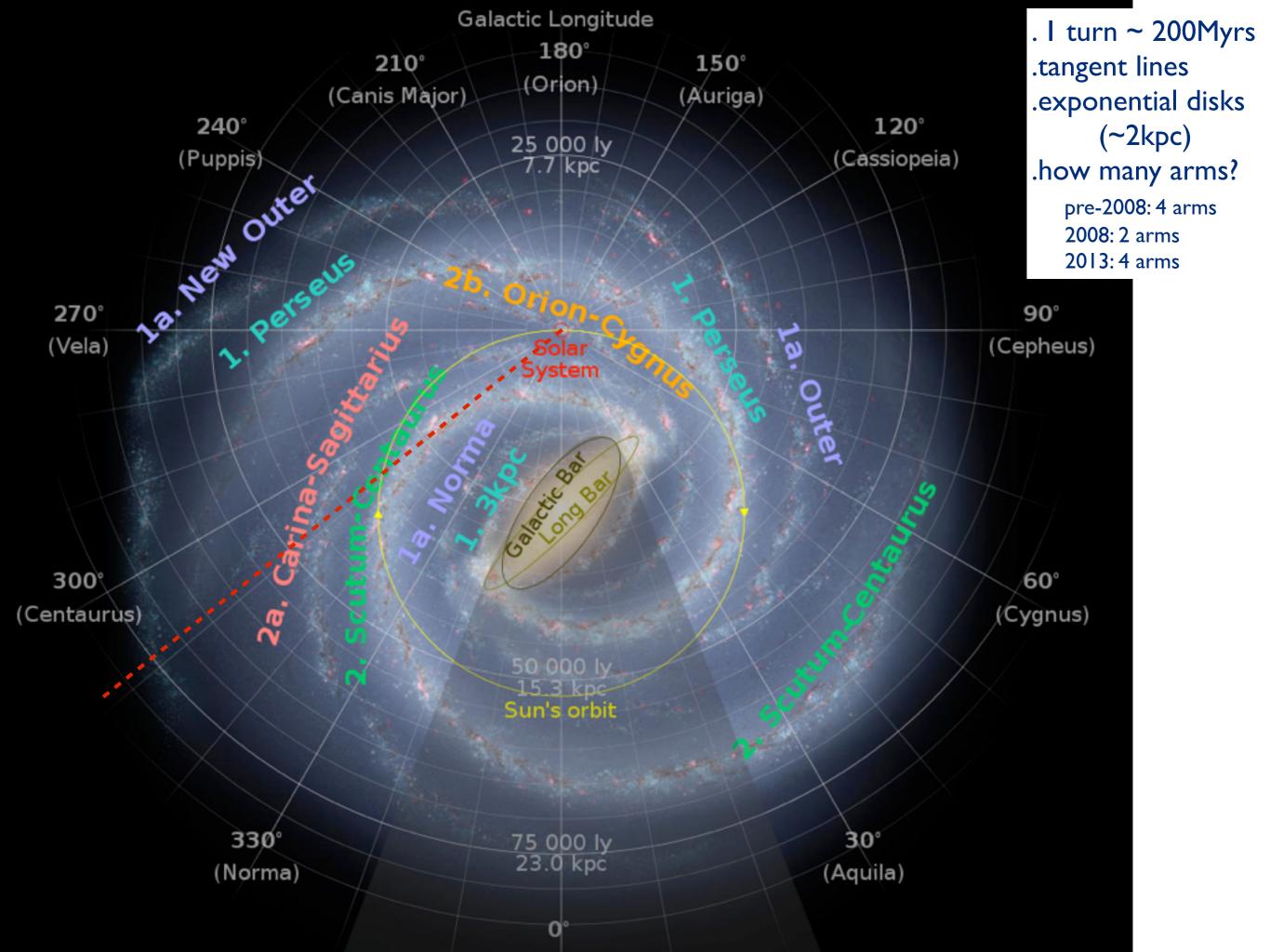


Radio (0.4 GHz) Atomic Hydrogen Radio (2.7 GHz) Molecular Hydrogen Infrared mm Mid Infrared Near Infrared micron Optical X-Ray nm Gamma Ray

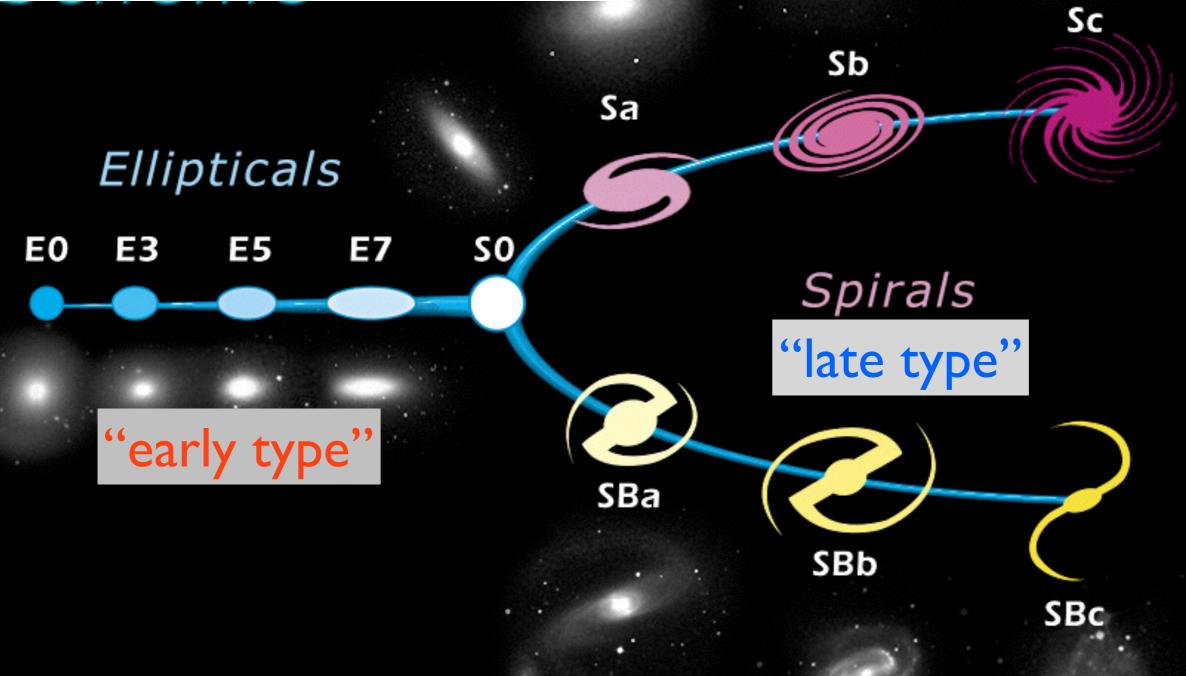


# Dust map (projected on ecliptic plane)





# Hubble sequence (Hubble's tuning fork)



MW

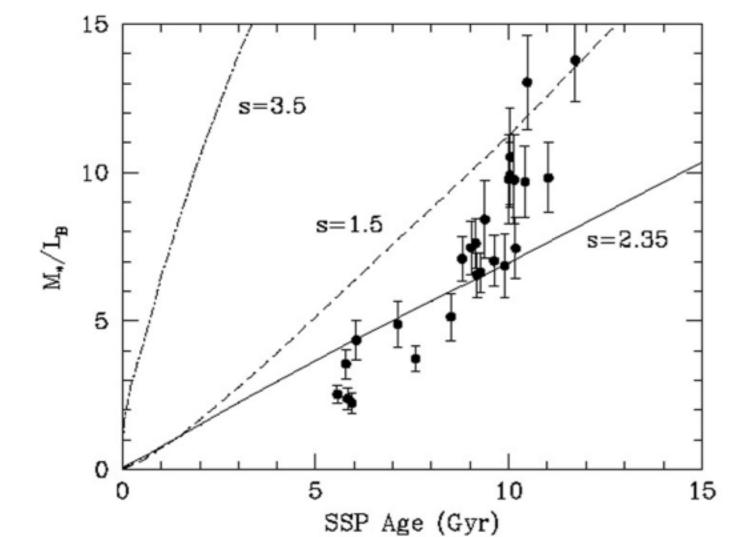
+ Irregular galaxies

# Mass-to-light ratio of stellar systems

### the Sun:

$$\label{eq:mass} \begin{split} \text{mass} = 1 M_{\odot}, \ \text{Lumin} = 1 L_{\odot}, \quad \text{mass/light} = 1 \ [M_{\odot}/L_{\odot}] \\ \text{on main-sequence, light ~ mass^4} \\ \text{B2 main-sequence star: mass/light = 0.002} \\ \text{M2 main-sequence star: mass/light = 12.5} \end{split}$$

In a co-eval population of stars, mass/light increases with age.



theory: straight lines s is slope for IMF, larger s means more dwarves s=2.35: Salpeter IMF

data: local ellipticals

Greggio & Renzini 'II

# Measured mass-to-light ratios locally:

Table 1.1 Inventory of the solar neighborhood

BT Chap. I

component	volume	luminosity		
	density	density		
	$({\cal M}_\odot{ m pc}^{-3})$	$(L_{\odot}\mathrm{pc}^{-3})$	M/L	
visible stars	0.033	0.05	~	
stellar remnants	0.006	0	0	
brown dwarfs	0.002	0	0	
ISM	0.050	0	0	
total	$0.09 \pm 0.01$	0.05	~2	
dynamical	$0.10 \pm 0.01$		~2	

NOTES: Volume and luminosity densities are measured in the Galactic midplane and surface density is the total within  $\pm 1.1$  kpc of the plane. Luminosity density and surface brightness are given in the R band. Dynamical estimates are from §4.9.3. Most other entries are taken from Flynn et al. (2006).

visible stars: alpha-Centauri system at 1.3 pc, so 0.2 star/pc<sup>3</sup>, or ~ 0.1  $M_{sun}/pc^3$  ISM:  $n_H \sim 1/cm^3$ , so ~ 0.1  $M_{sun}/pc^3$  solar neighbourhood  $M/L_R \sim 2$  (~ 2.5 if integrated to +/- 1.1 kpc)

all mass explained in our immediate neighbourhood

# Measured mass-to-light ratios locally: (extend to +/- I.Ikpc)

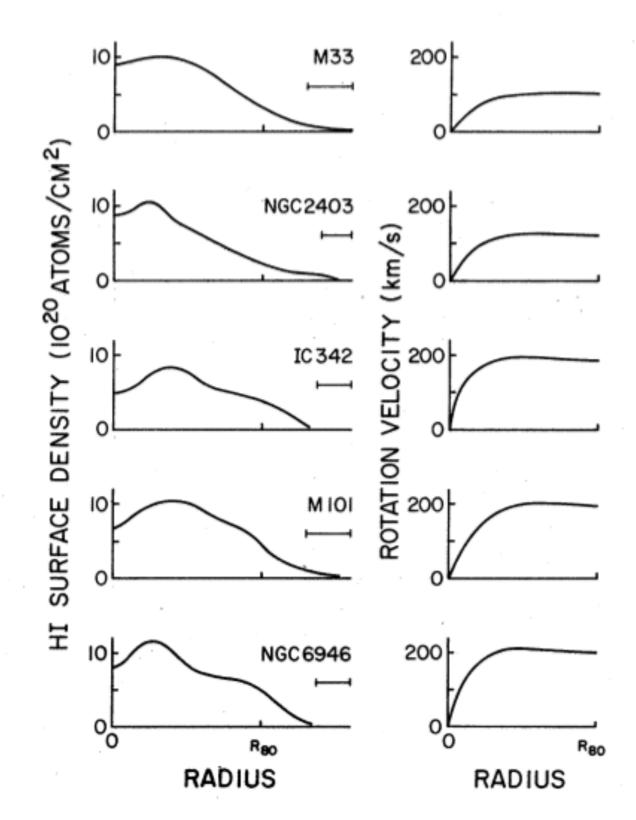
Table 1.1 Inventory of	the solar neighborhood	BT Chap.	<u>1</u>
component	surface	surface	_
	density	brightness	
	$({\cal M}_{\odot}{ m pc}^{-2})$	$(L_{\odot}\mathrm{pc}^{-2})$	M/L
visible stars	29	29	~
stellar remnants	5	0	0
brown dwarfs	2	0	0
ISM	13	0	0
total	$49 \pm 6$	29	~2
dynamical	$74\pm 6$	_	~3

NOTES: Volume and luminosity densities are measured in the Galactic midplane and surface density is the total within  $\pm 1.1$  kpc of the plane. Luminosity density and surface brightness are given in the R band. Dynamical estimates are from §4.9.3. Most other entries are taken from Flynn et al. (2006).

vertically (to +/-1.1kpc)
unexplained matter ~ explained matter

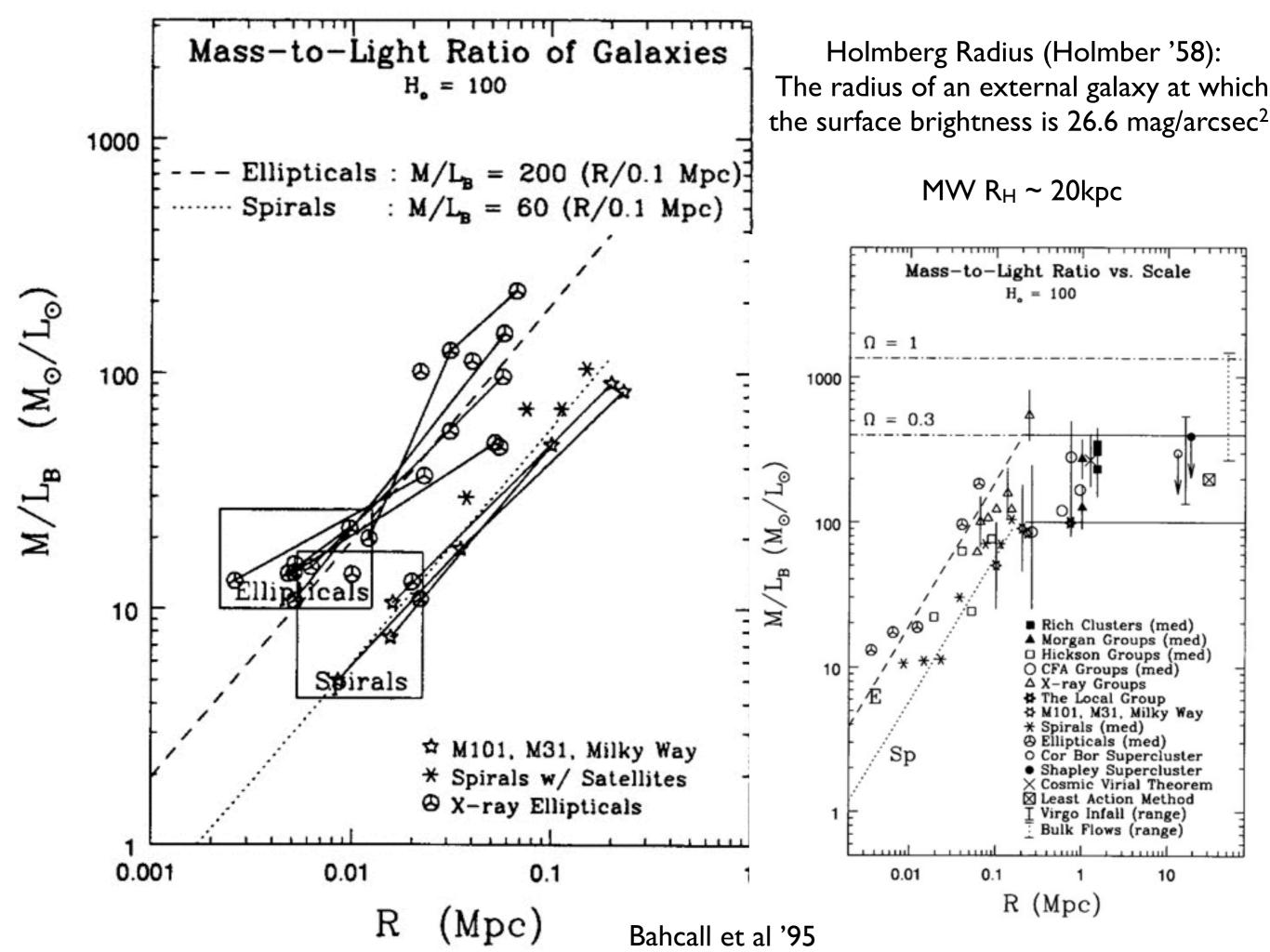
How to measure mass-to-light ratio? -- whole galaxy

### Galactic Rotation Curves

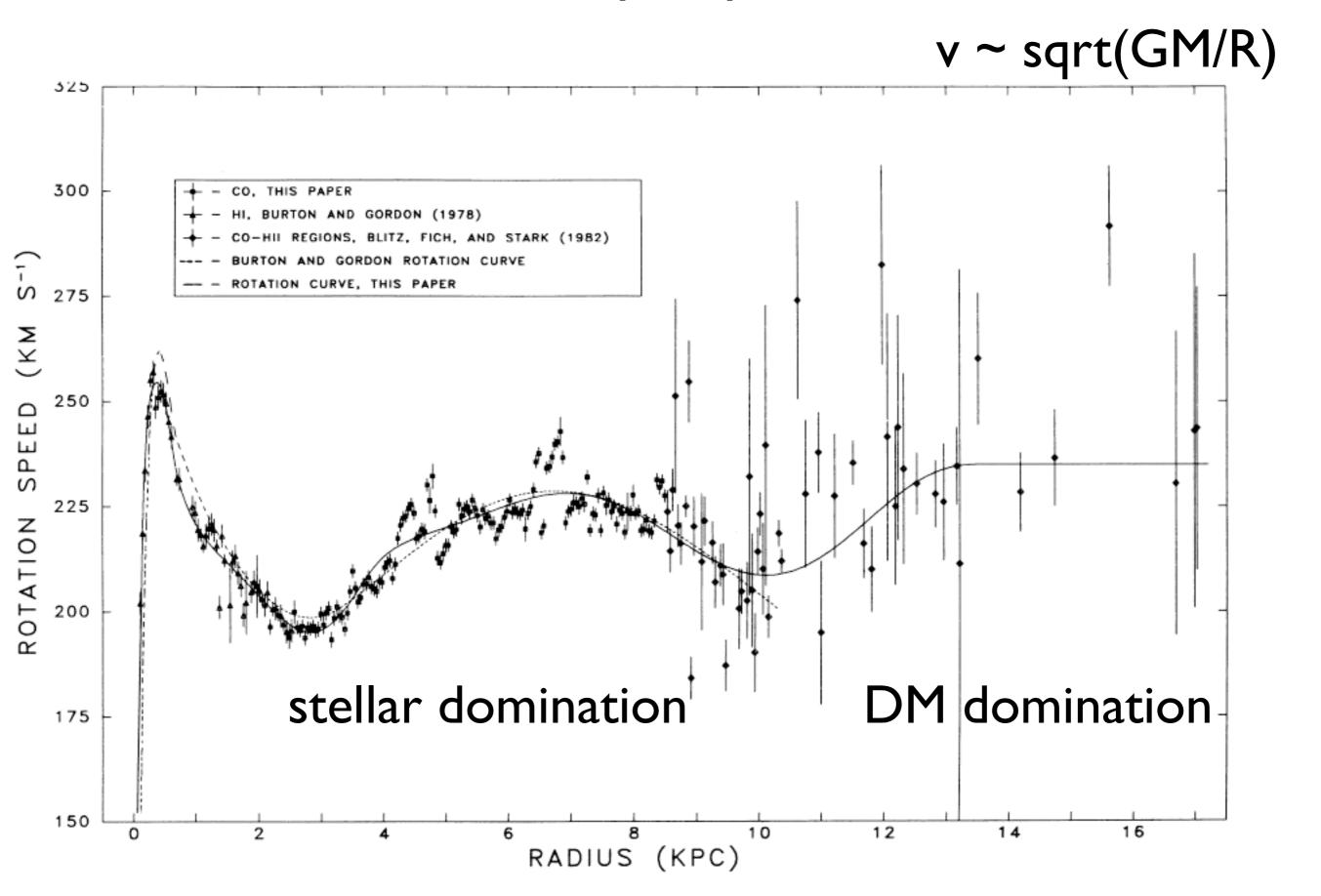


Rogstad & Shostak '72

Fig. 1.—Azimuthally averaged hydrogen surface densities and rotation velocities for five Scd galaxies. These curves were obtained by appropriate smoothing of the two-dimensional maps. The bars under alaxy names indicate average radial beam diameters.  $R_{80}$  is the radius within which is found 80 percent f the observed H I.



### Rotation curve of the Milky Way (Clemens '85)



### EQUILIBRIUM DISK-BULGE-HALO MODELS FOR THE MILKY WAY AND ANDROMEDA GALAXIES

#### LAWRENCE M. WIDROW

Department of Physics, Queen's University, Kingston, ON K7L 3N6, Canada; widrow@astro.queensu.ca

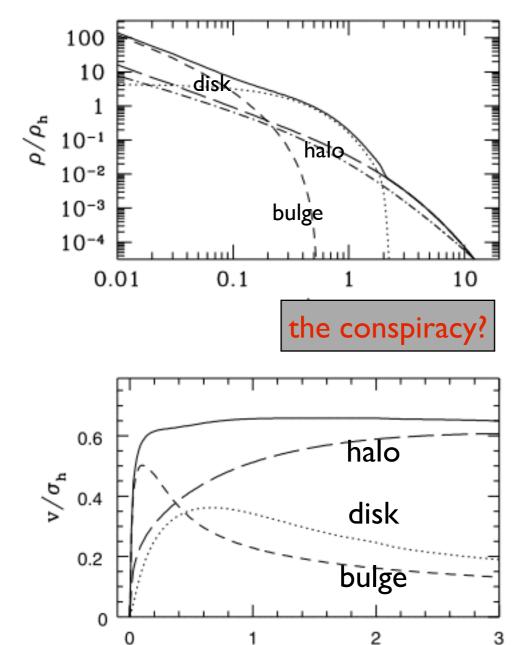
#### AND

#### JOHN DUBINSKI

Department of Astronomy and Astrophysics, University of Toronto, 60 St. George Street, Toronto, ON M5S 3H8, Canada; dubinski@astro.utoronto.ca Received 2005 January 27; accepted 2005 June 11

#### ABSTRACT

new set of self-consistent, equilibrium disk galaxy models that incorporate an exponential disk, a bulge, an NFW halo, and a central supermassive black hole. The models are derived from explicit ions for each component, and the large number of parameters permit detailed modeling of actual ent techniques that use structural and kinematic data such as radial surface brightness profiles, robulge velocity dispersion profiles to find the best-fit models for the Milky Way and M31. Through ns of these models we explore their stability against the formation of bars. The models permit the ange of dynamical phenomenon with a high degree of realism.



Annu. Rev. Astron. Astrophys. 1991. 29: 409-45 Copyright © 1991 by Annual Reviews Inc. All rights reserved

### THE MASS OF THE GALAXY

### Michel Fich

Guelph-Waterloo Program for Graduate Work in Physics, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada

### Scott Tremaine

Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, Ontario M5S 1A1, Canada

Fig. 2.—Density profile (top) and rotation curve (bottom) for the diskbulge-halo model described in the text. Shown are the contributions from the disk (dotted line), bulge (dashed line), halo (long-dashed line), as well as the total density profile and rotation curve (solid line). Also shown is the halo model that results if the same halo parameters are used and the disk and bulge are not included (dot-dashed line in the top panel).

r/a<sub>h</sub>

# DISTRIBUTION OF DARK MATTER IN NGC 3198 van Albada et al. '85 NGC 3198 150 halo V<sub>cir</sub> (km/s) 100 disk Radius (kpc)

decomposition nonunique (dep. on disk M/L value)

disk exponential, with scale length (in light) ~ 3kpc

ial disk with maximum mass and halo to observed rotation curve (dots with error bars). The scale length of the ion (60", corresponding to 2.68 kpc). The halo curve is based on eq. (1), a = 8.5 kpc,  $\gamma = 2.1$ ,  $\rho(R_0) = 0.0040 M_{\odot}$ 

# disk-halo conspiracy? something important about galaxy formation

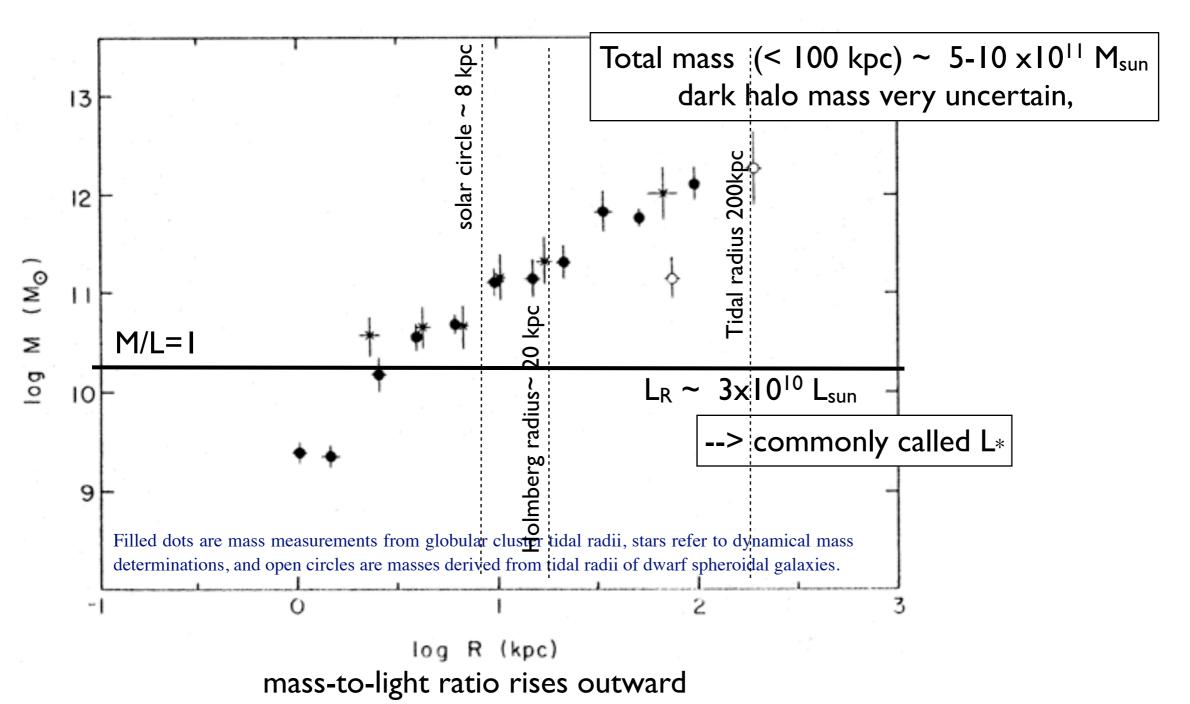
 $R_0$  equal to 8 kpc. This allows a comparison of  $\rho_{\rm halo}(R_0)$  for the models with the halo mass density in the solar neighborhood ( $\sim 0.01$ – $0.02~M_{\odot}~{\rm pc}^{-3}$ ; Bahcall and Soneira 1980). Equation (1) is equivalent to

$$\rho_{\text{halo}}(R) = \rho_{\text{halo}}(0) \left[ 1 + \left( \frac{R}{a} \right)^{\gamma} \right]^{-1}.$$

MW @ 8kpc disk: 0.1M\_sun/pc^3 halo: 0.01 M sun/pc^3

# Enclosed mass in the Milky Way

### methods other than rotation curves



Milky way M/L<sub>R</sub> (< 100kpc)  $\sim 15 - 30$  (BT quotes 7-170)

galaxy clusters (average in universe) ~ 200

# an L\* galaxy is typical in the universe -- the Schechter Luminosity function

$$\Phi(L) \ dL = n_* \ \left(\frac{L}{L_*}\right)^{\alpha} exp\left(-\frac{L}{L_*}\right) \ d\left(\frac{L}{L_*}\right)$$

Press & Schechter '74 Schechter '76

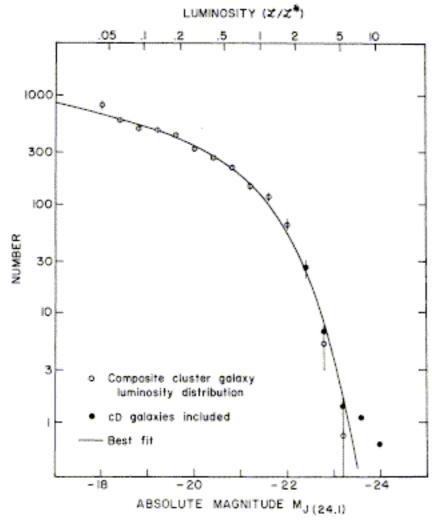
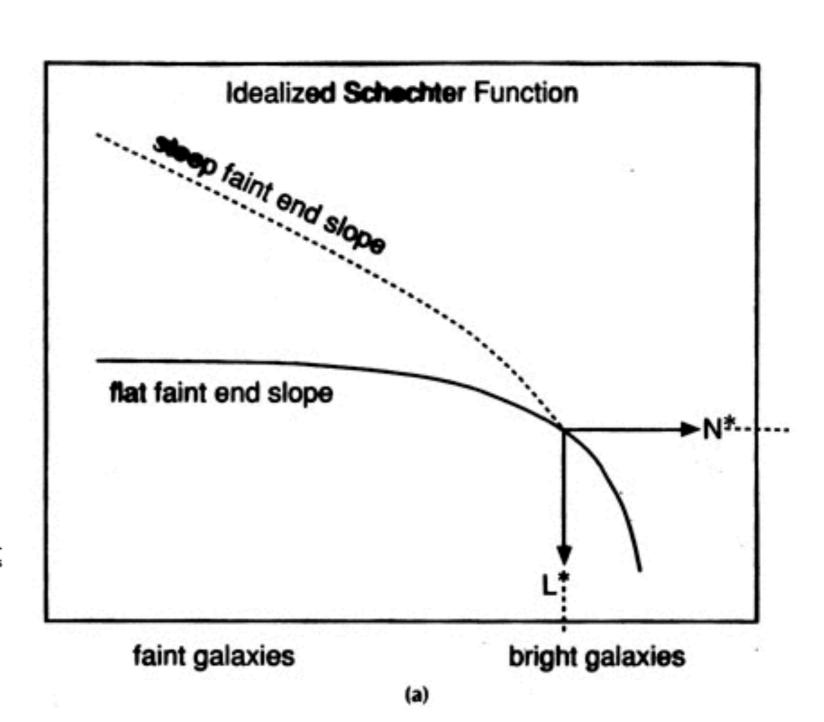


Fig. 2.—Best fit of analytic expression to observed composite cluster galaxy luminosity distribution. Filled circles show the effect of including cD galaxies in composite.



While dark matter cosmology seems well established, one remaining central challenges is to understand how galaxies form.

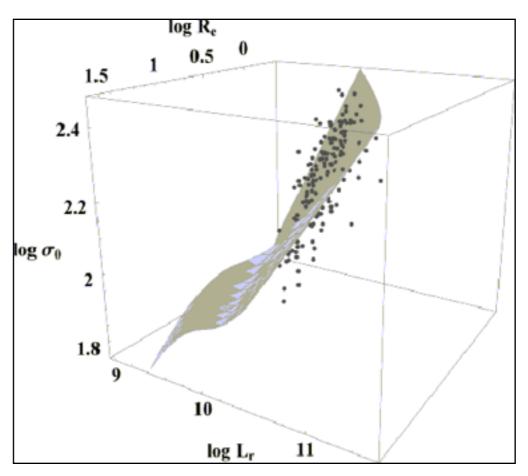
Theory vs. Observations:

. global properties

. individual components

### Fundamental planes:

some properties of a galaxy that are observed to correlate with other properties.



### examples:

the Faber-Jackson law -- velocity dispersion/Luminosity the Tully-Fisher law -- rotation velocity/Luminosity the Kormendy relation -- surface brightness/size the M-sigma relation -- central blackhole mass/dispersion

# The Tully-Fisher Relation for disk galaxies

 $L \propto V^{\alpha}$ 

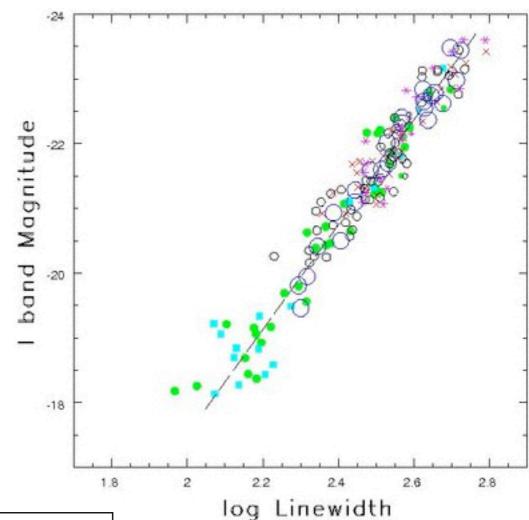
L: galaxy luminosity,

V: characteristic velocity (rotation velocity)

 $\alpha_B \approx 3.5, \, \alpha_{\rm IR} \approx 4$ 

V is set by the DM halo, L is set by luminous matter

scatter ~ 0.2 mag good enough for distance ladder

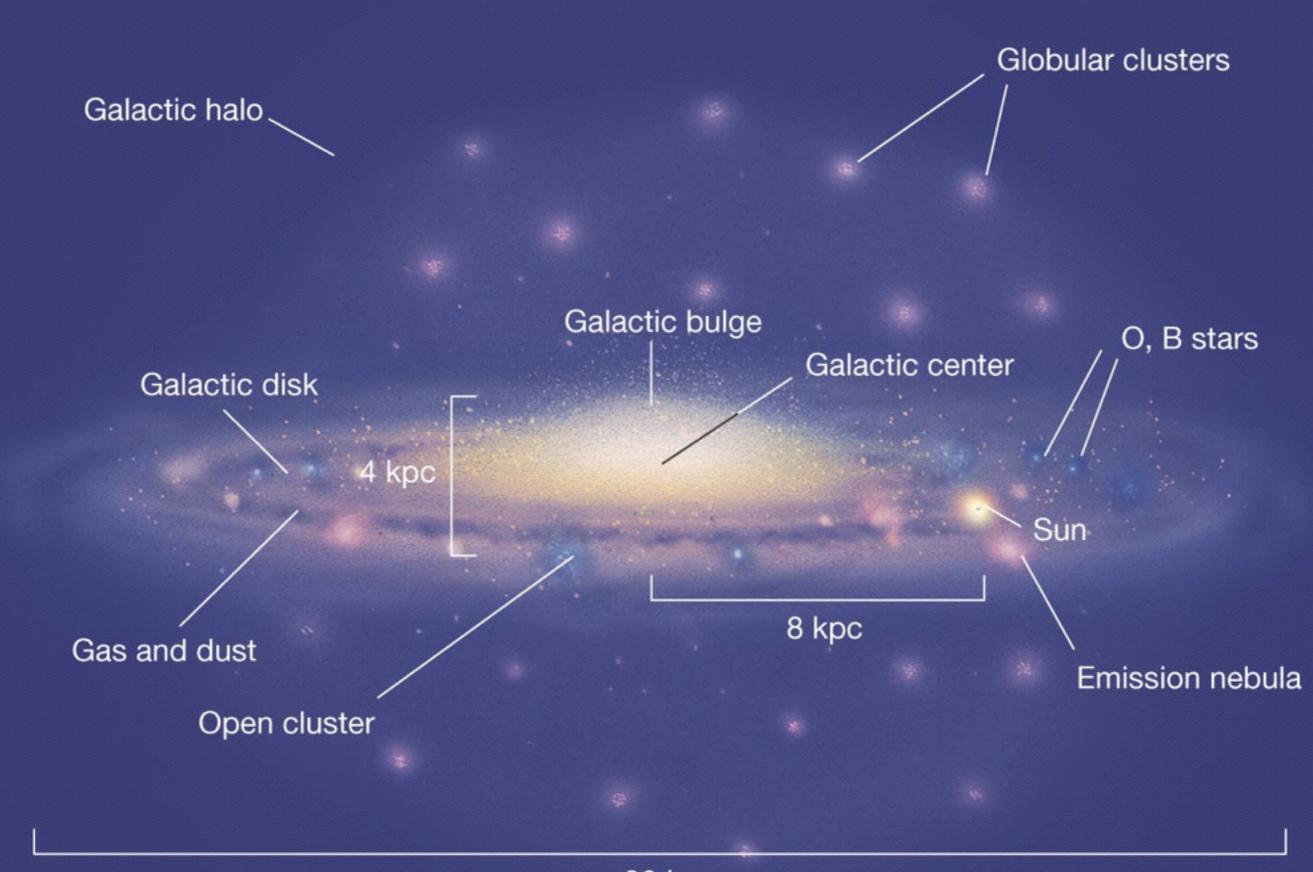


Let 
$$v^2 \approx \frac{GM}{R}$$
 (Virial Theorem)  
 $M = (M/L) \times L = \gamma L$ , where  $\gamma$  is the mass-to-light ratio  $L \approx \frac{V^2 R}{G \gamma}$ 

So 
$$\frac{M}{R^2} \propto \frac{1}{\gamma}$$

dark matter halo knows about the mass-to-light ratio

# Components of the Galaxy



# multiple components in the MW & the assembly history

- geometry of MW (thin/thick disks+bulge+halo, the distribution of star light)
- dark matter dominates at large distances (rotation curve)
- the local group (distance to LMC, SMC, dwarf galaxies, missing satellites)
- globular clusters (double MS, mass segregation)
- galactic center (BH, stellar cluster),

A correct assembly history produces these components, and explains the observed fundamental planes.

# How many stars are in the MW?

Table 1.2 Properties of the Galaxy

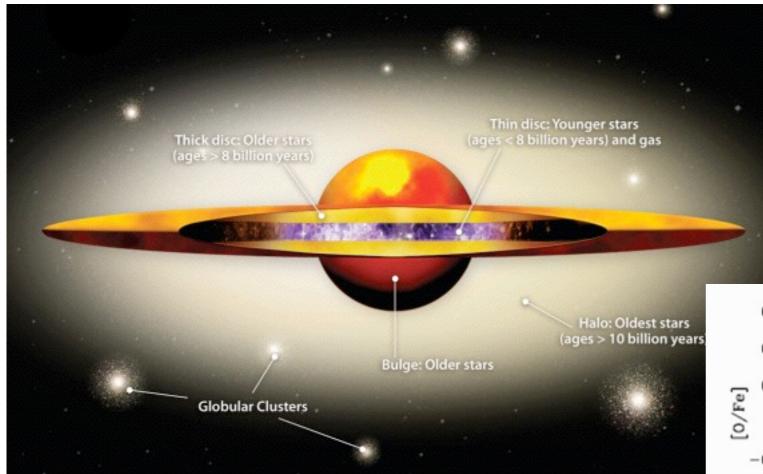
BT

Global properties:				
disk scale length $R_{\rm d}$	$(2.5 \pm 0.5)  \rm kpc$			
disk luminosity	$(2.5 \pm 1)  imes 10^{10}  L_{\odot}$			
bulge luminosity	$(5 \pm 2) \times 10^{9} L_{\odot}$			
total luminosity	$(3.0 \pm 1) \times 10^{10} L_{\odot}$			
disk mass	$(4.5 \pm 0.5) \times 10^{10}  M_{\odot}$			
bulge mass	$(4.5 \pm 1.5) \times 10^9  M_{\odot}$			
dark halo mass	$(2^{+3}_{-1.8}) \times 10^{12}  \mathcal{M}_{\odot}$			
dark halo half-mass radius	$(100^{+100}_{-80}) \mathrm{kpc}$			
disk mass-to-light ratio $\Upsilon_R$	$(1.8 \pm 0.7)\Upsilon_{\odot}$			
total mass-to-light ratio $\Upsilon_R$	$(70^{+100}_{-63})\Upsilon_{\odot}$			
black-hole mass	$(3.9 \pm 0.3) \times 10^6  \mathcal{M}_{\odot}$			
Hubble type	Sbc			

stellar halo mass (Bell et al '07)  $(3.7 \pm 1.2) \times 10^8 M_{\odot}$ 

$$(3.7 \pm 1.2) \times 10^8 M_{\odot}$$

# Stellar Disk(s), 90%: thin + thick

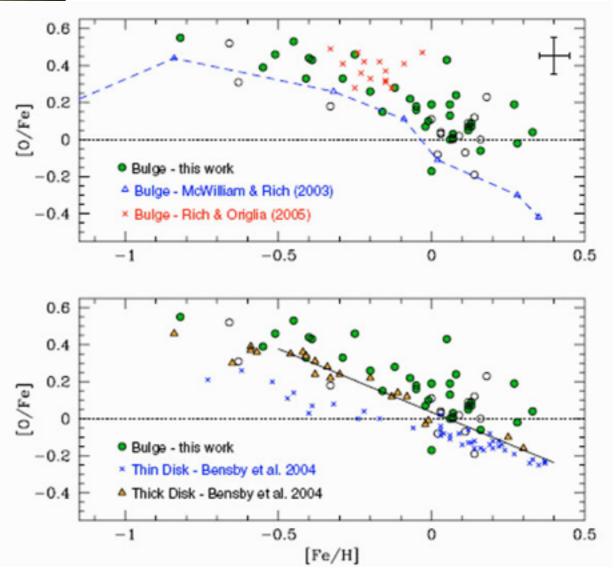


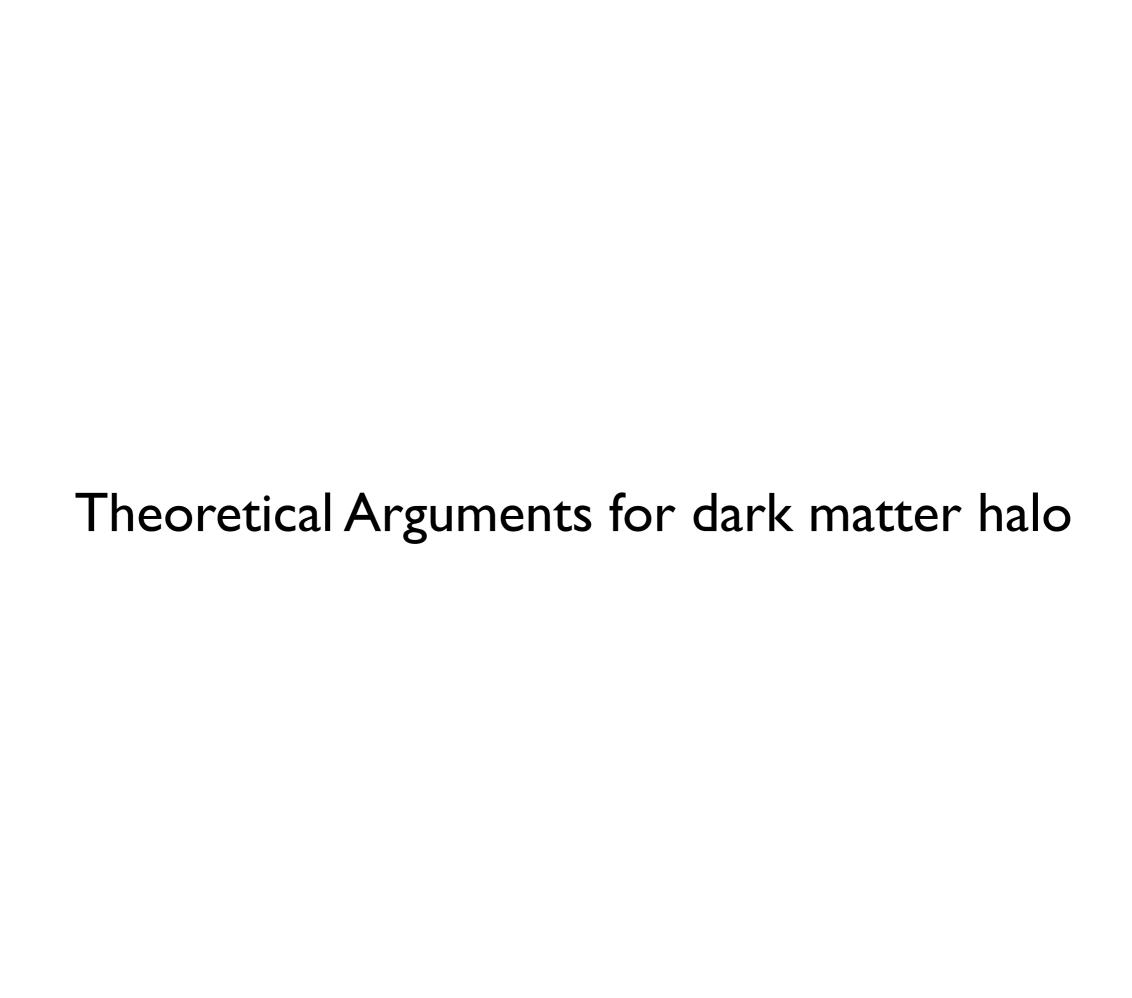
•stars formed in disks (why?)

- •we have two roughly equal mass disks (Gilmore & Reid 1983, arXiv1401.1835)
- •vertical scale height: thin ~300pc; thick ~ Ikpc; radial scale length, thin ~ 3.6kpc, thick ~ 2kpc;
- thick disk exclusively old stars,
- different metallicity distributions
- •the Sun is a thin-disk star

origin of thick disk:

thin disk flattening up? early star formation different? mergers and stirrings?





### Can a thin disk of stars be stable?

### ON THE GRAVITATIONAL STABILITY OF A DISK OF STARS

### Alar Toomre

Department of Mathematics, Massachusetts Institute of Technology Received August 17, 1963; revised January 18, 1964

### ABSTRACT

This paper considers the question of the large-scale gravitational stability of an arbitrary, highly flattened stellar system, which is assumed initially to rotate in approximate equilibrium between its self-gravitation and the centrifugal forces. It is concluded that no such disk, if fairly smooth or uniform, can be entirely stable against a tendency to form massive condensations within its own plane, unless the root-mean-square random velocities of its constituents, in the directions parallel to that plane, are everywhere sufficiently large. Lacking such random motions, it is shown that the system must be vulnerable to numerous unstable disturbances, the dimensions of which may approach its over-all radius, and whose times of growth are to be reckoned in fractions of the typical periods of revolution.

The minimum root-mean-square radial velocity dispersion required in any one vicinity for the complete suppression of all axisymmetric instabilities is calculated (in collaboration with A. Kalnajs) as 3.36  $G\mu/\kappa$ , where G is the gravitational constant, and  $\mu$  and  $\kappa$  are the local values of the projected stellar density and the epicyclic frequency, respectively. From that, and the observed  $\mu$  and  $\kappa$ , together with their uncertainties, this minimum for the solar neighborhood of our Galaxy is estimated to fall between 20 and 35 km/sec, a range which indeed encompasses the actual radial velocity dispersions of the most predominant types of stars in our vicinity. It is pointed out that both this curious agreement, and also the well-known discrepancy between the z- and r-velocity dispersions at least of the older disk stars, may be explainable in terms of past instabilities of this galactic disk.

### Toomre said: not infinitely thin.

Ostriker & Peebles said: need dark matter halo

A NUMERICAL STUDY OF THE STABILITY OF FLATTENED GALAXIES: OR, CAN COLD GALAXIES SURVIVE?\*

J. P. OSTRIKER

Princeton University Observatory

AND

### P. J. E. PEEBLES

Joseph Henry Laboratories, Princeton University Received 1973 May 29

# T= rotational energy W=grav. energy

# rotationally supported T/|W| = 0.5

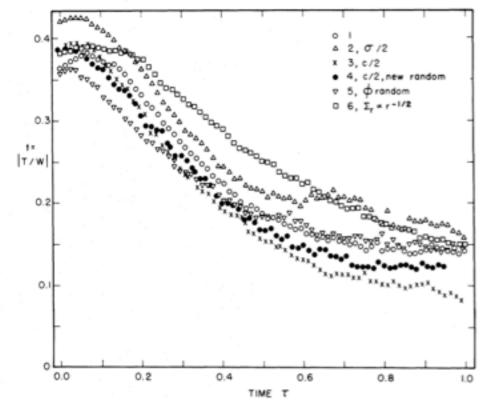


Fig. 2.—Evolution of the model galaxies. Abscissa is time measured in units of the orbit period r the outermost particles in the initial system under the assumption of circular orbits. Ordinate defined in equation 3.

#### ABSTRACT

To study the stability of flattened galaxies, we have followed the evolution of simulated galaxies containing 150 to 500 mass points. Models which begin with characteristics similar to the disk of our Galaxy (except for increased velocity dispersion and thickness to assure local stability) were found to be rapidly and grossly unstable to barlike modes. These modes cause an increase in random kinetic energy, with approximate stability being reached when the ratio of kinetic energy of rotation to total gravitational energy, designated t, is reduced to the value of  $0.14 \pm 0.02$ . Parameter studies indicate that the result probably is not due to inadequacies of the numerical N-body simulation method. A survey of the literature shows that a critical value for limiting stability  $t \simeq 0.14$  has been found by a variety of methods.

Models with added spherical (halo) component are more stable. It appears that halo-to-disk mass ratios of 1 to  $2\frac{1}{2}$ , and an initial value of  $t \simeq 0.14 \pm 0.03$ , are required for stability. If our Galaxy (and other spirals) do not have a substantial unobserved mass in a hot disk component, then apparently the halo (spherical) mass *interior* to the disk must be comparable to the disk mass. Thus normalized, the halo masses of our Galaxy and of other spiral galaxies *exterior* to the observed disks may be extremely large.

Subject headings: galactic

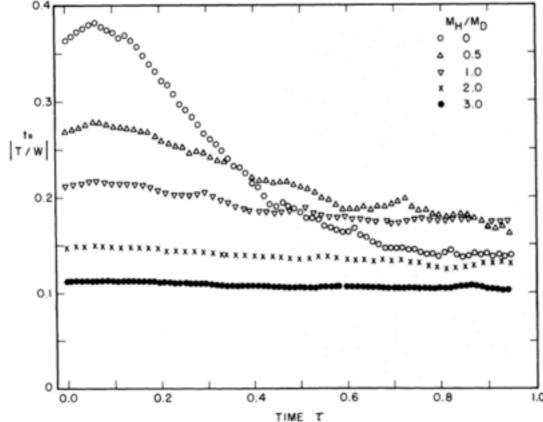
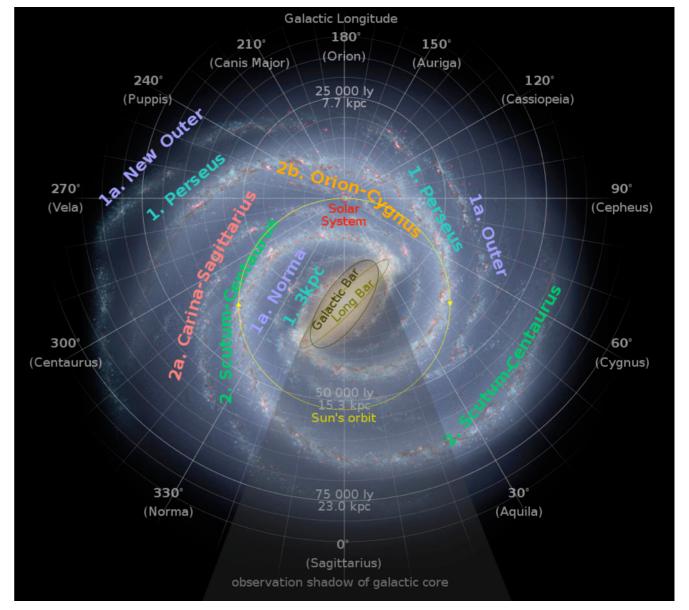


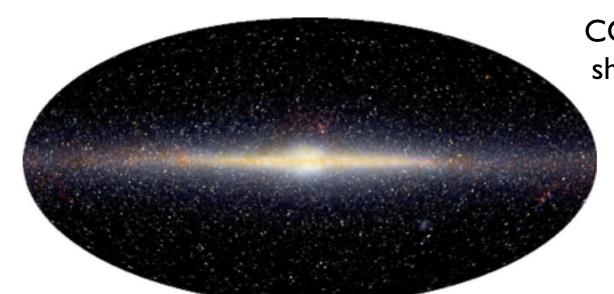
Fig. 6.—Effect of the halo on the evolution of the model galaxy

Spiral arms: compression of stars and ISMs



- .ISM compression leads to star formation. So young stars are found in spiral arms.
- .oddly, old disk stars are organized into 2-arm spirals('08) while young stars 4-arm ('13)
- . are spiral arms long lived or transient?
- . are spiral arms externally excited?

Bulge stars, 10%:



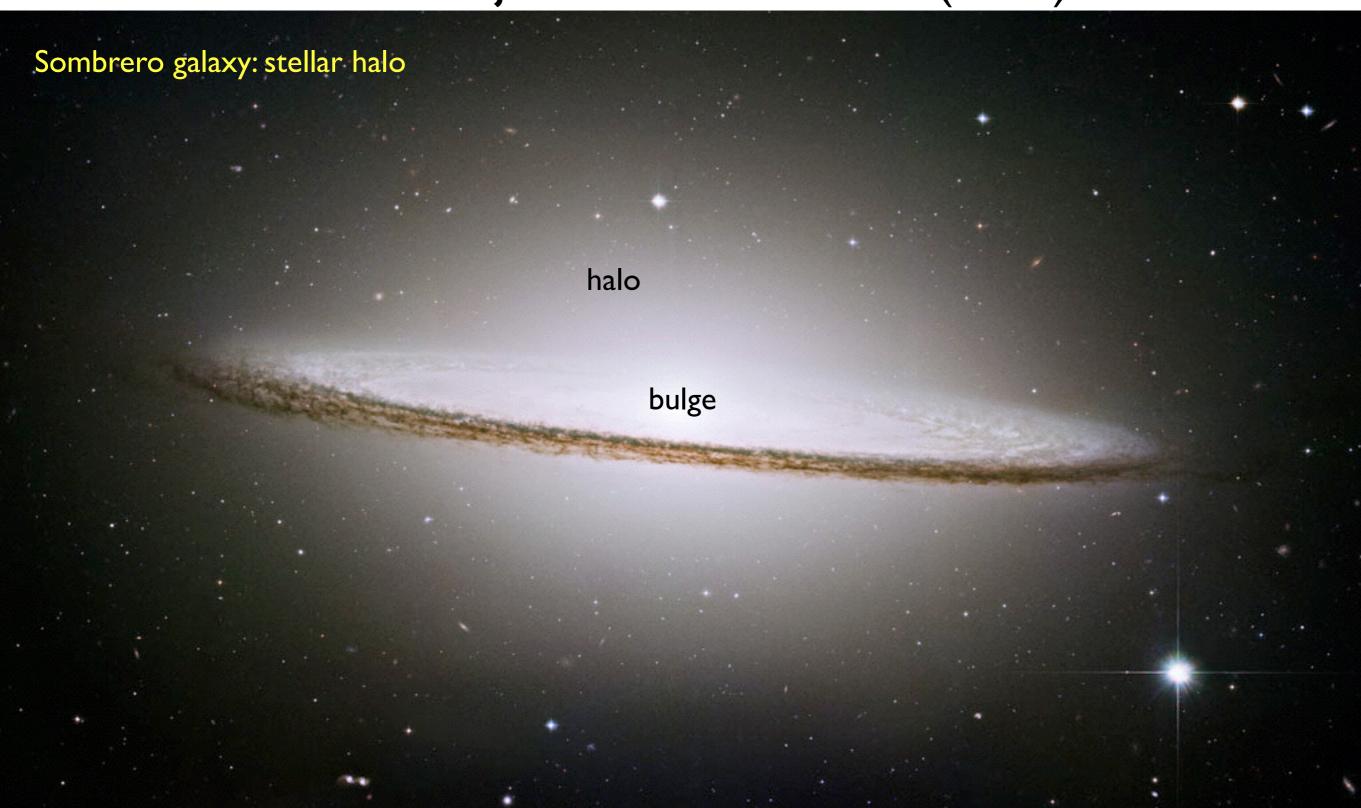
COBE map of MW showing the bulge

.vertical thickening of stars near the center (< 3kpc)

- . common among disk galaxies
- . some are classical bulges (mini-ellipticals), some are pseudo-bulges (bars)
- . we have a long bar
- . stars old (> 12 Gyrs), with a span of metallicities
- . formation not understood: merger? secular process? (little dark matter there)
- . central region hosts massive blackholes

Halo stars, 1%:

halo likely from accreted dwarfs, as well as some stars ejected from center (HVS)



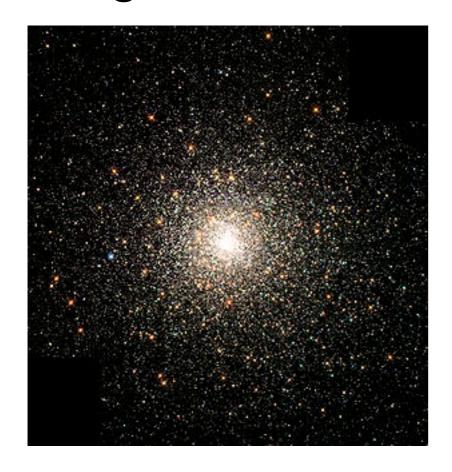
### The halos are studded with Globular Clusters

### globular cluster:

~ 10^5 stars, invariably old (in MW) age ~ 10^4 dynamical time (typical galaxy/cluster ~a few) central density: 10^4 M\_sun/pc^3

(solar neighbourhood: ~ 0.1 M\_sun/pc^3)

### Origin unclear



MW: ~200

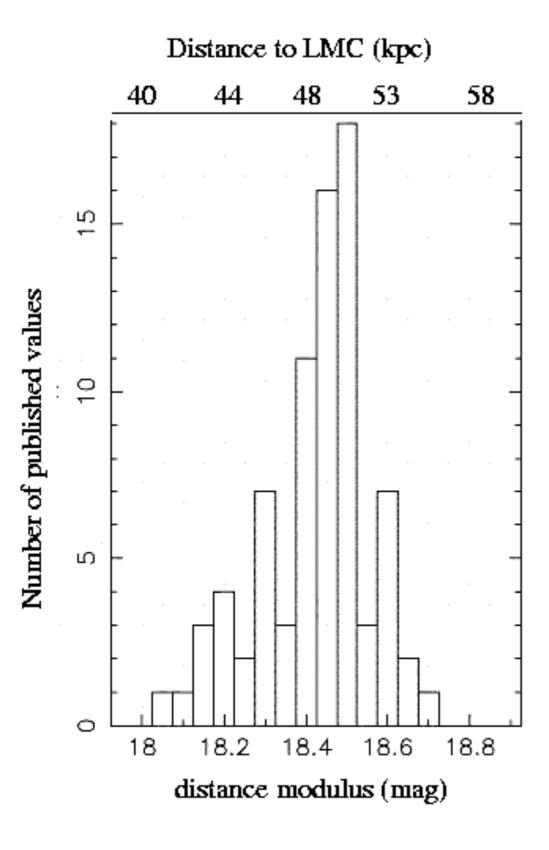
Andromedae: ~ 500

M87: ~ 13,000

# LMC/SMC



## Distance to LMC/SMC

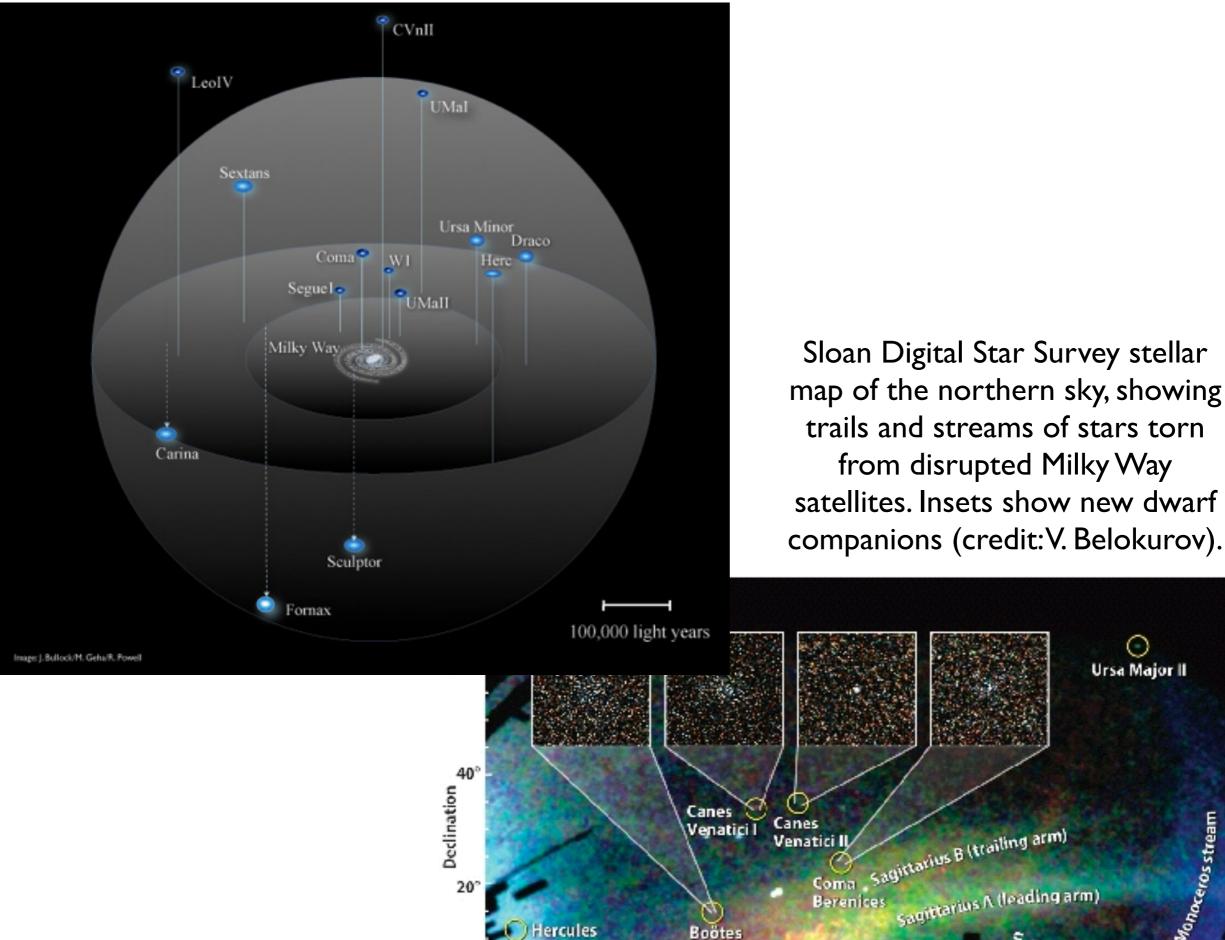


LMC distance sets the calibration of Cepheids, so affects all cosmological distance measurements, 10% error

methods include: RR Lyrae, Tip red giant, Mira, SN 1987A, main sequence fitting, eclipsing binary, red clump

$$d = 10^{\frac{\mu}{5}+1}$$
 distance modulus

HST team compiled previous data: 18.5+/-0.1 mag ('01) later results tend to aggregate (Schaefer '08)



Leo IV

# "Missing Satellite Problem"

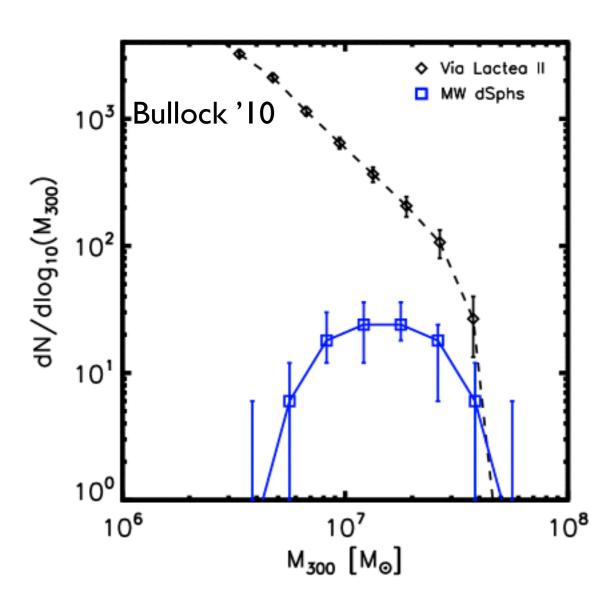


Fig. 1.11. Luminosity function of dSph galaxies within  $R_{\rm h}=417$  kpc of the Su as observed (lower), corrected for only SDSS sky coverage (middle), and with h minosity completeness corrections from Tollerud et al. (2008) included (upper Note that the brightest, classical (pre-SDSS) satellites are uncorrected, while ne satellites have the correction applied. The shaded error region corresponds to the 98% spread over mock observation realizations within the Via Lactea I halo.

L[Lo]

Combined Correction

• • Uncorrected/Observed

Fixed Coverage Correction

10<sup>4</sup>

10<sup>2</sup>

10

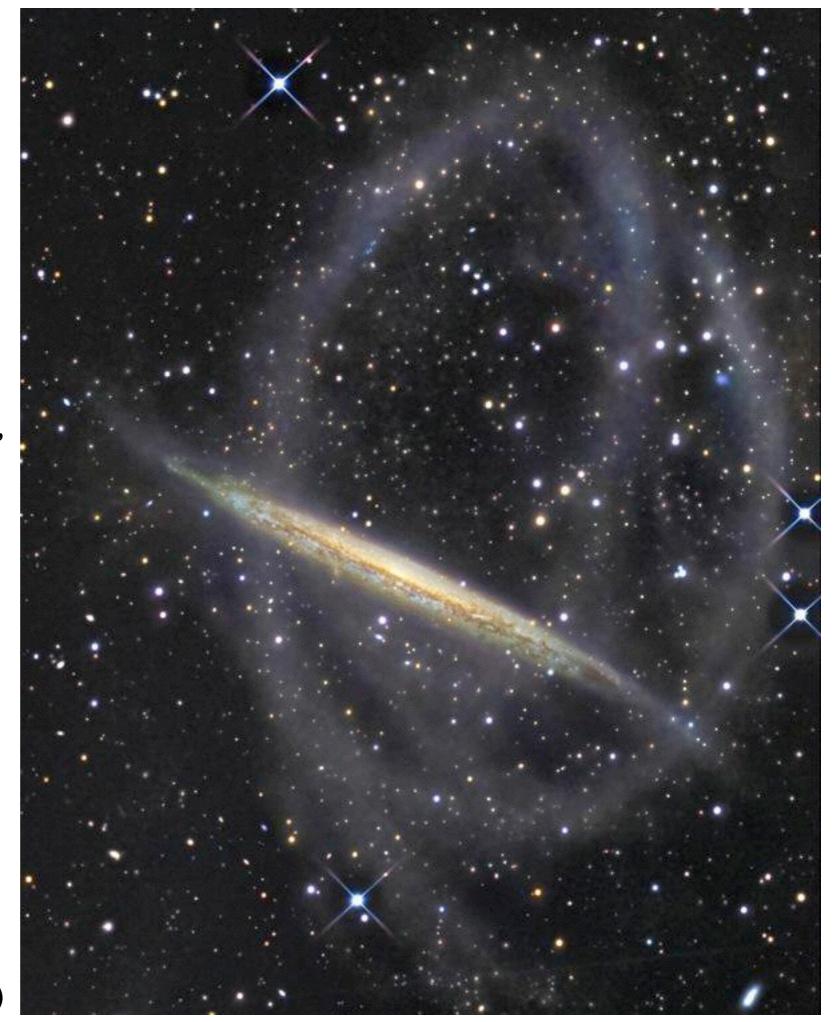
 $N(< M_V)$ 

Fig. 1.6. Mass function for  $M_{300} = M(<300 \mathrm{pc})$  for MW dSph satellites and subhalos in the Via Lactea II simulation within a radius of 400 kpc. The mind dashed curve is the subhalo mass function from the simulation. The solid curve the median of the observed satellite mass function. The error bars on the observed satellite mass function. The number of configuration that occur with a 98% of the time (from Wolf et al., in preparation). Note that mismatch is about  $\sim 1$  order of magnitude at  $M_{300} \simeq 10^7 \, M_{\odot}$ , and that it grows

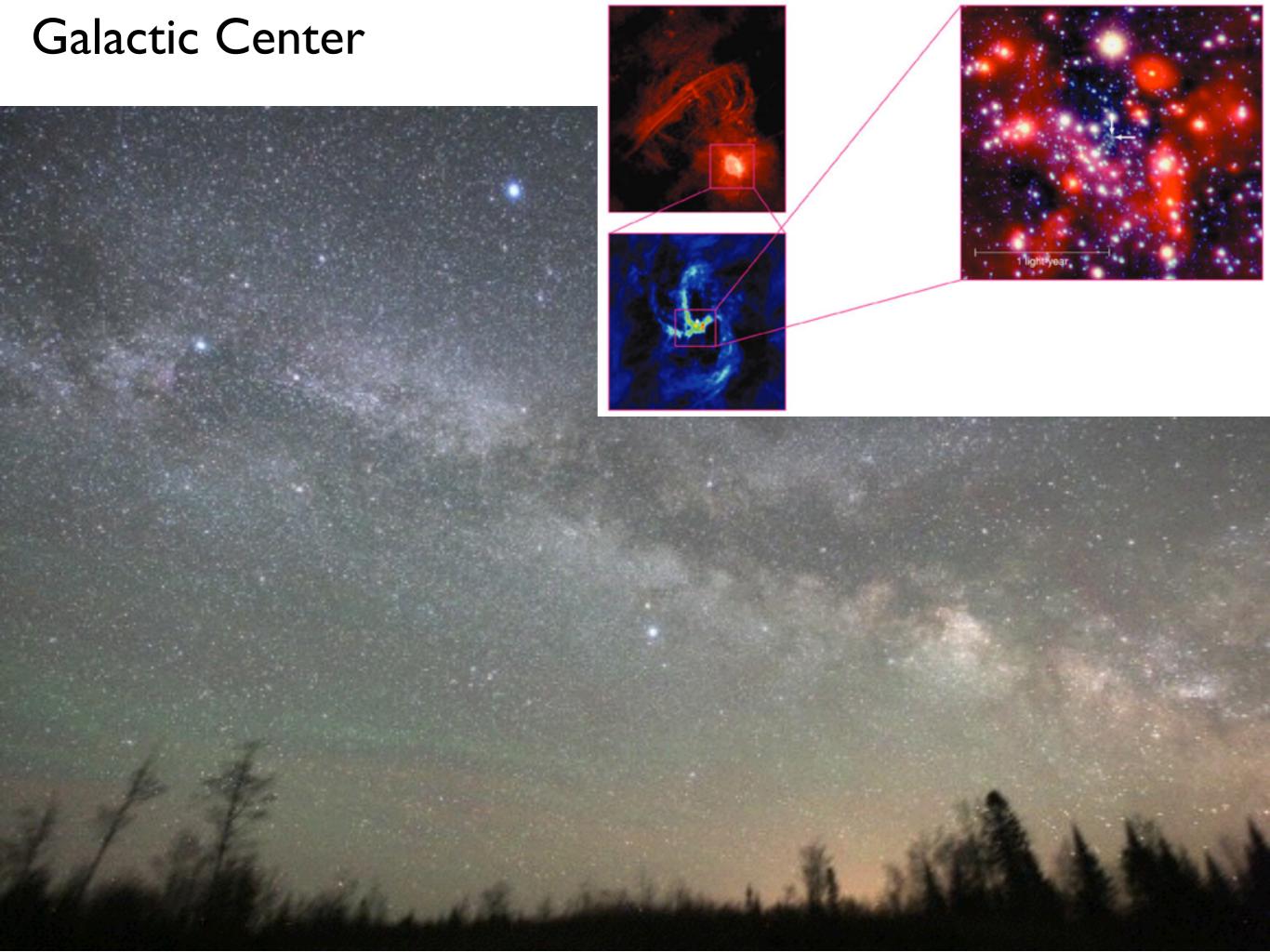
significantly towards lower masses.

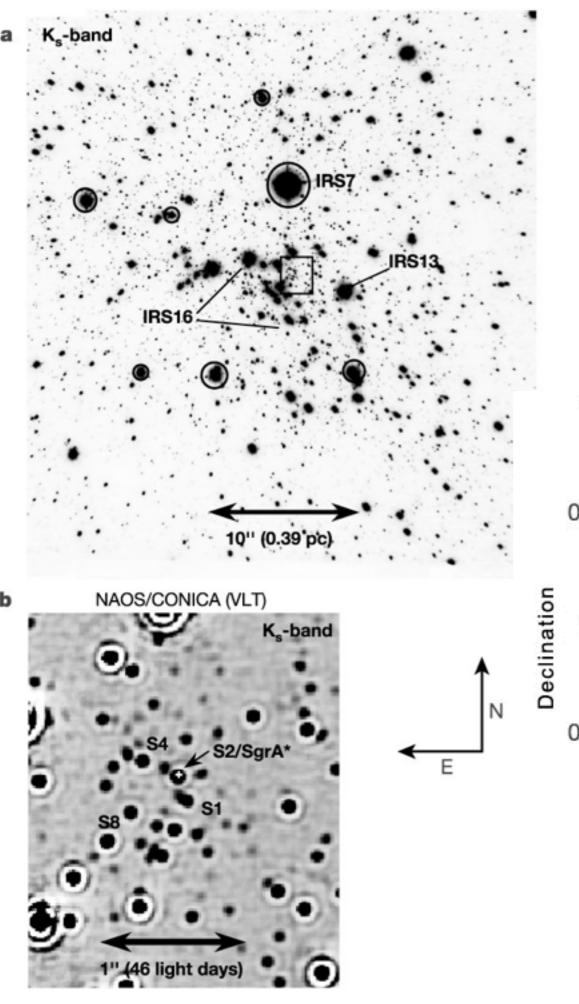
## Tidal Streams

dwarf galaxies incorporated into halos, tidal stripping shape of galactic potential (tri-axial?)



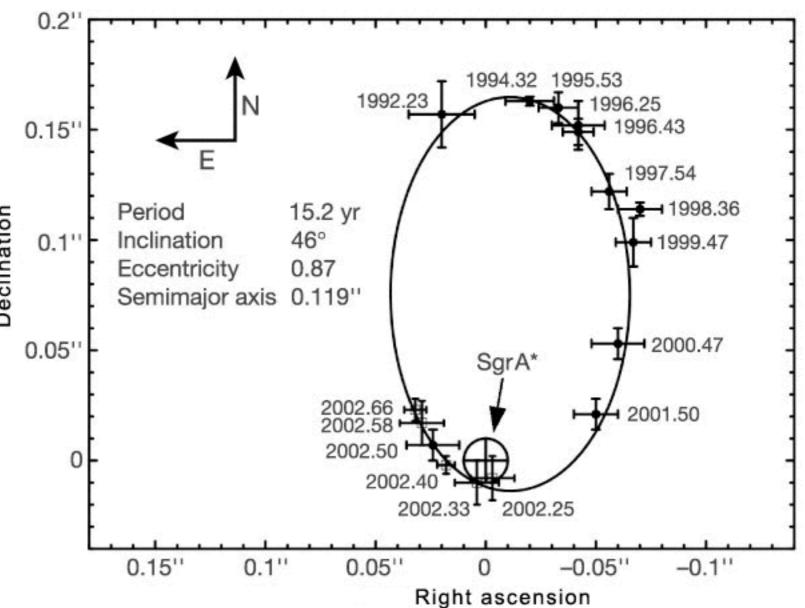
stellar tidal stream (NGC5907)





# Ks band image of the galactic center (Schodel et al '02)

Schodel et al '02, Ghez et al '05, Mbh = 3.7x10^6 M\_sun (R0/8kpc)^3



### A FUNDAMENTAL RELATION BETWEEN SUPERMASSIVE BLACK HOLES AND THEIR HOST GALAXIES

## Laura Ferrarese<sup>1</sup>

Department of Physics and Astronomy, UCLA, Los Angeles, CA 90095; laura@astro.ucla.edu

#### DAVID MERRITT

Department of Physics and Astronomy, Rutgers University, New Brunswick, NJ 08854; merritt@physics.rutgers.edu

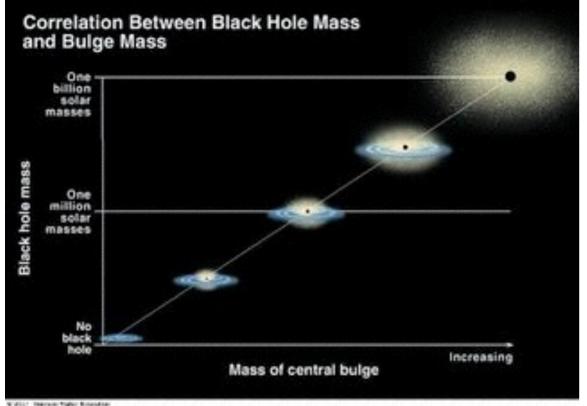
1900 citations

Received 2000 June 1; accepted 2000

### ABSTF

The masses of supermassive black holes correlate alm bulges,  $M_{\rm bh} \propto \sigma^{\alpha}$ , where  $\alpha = 4.8 \pm 0.5$ . The relation is luminosity, with a scatter no larger than expected on the recently estimated by Magorrian et al. lie systematically estimates, some by as much as 2 orders of magnitude. The between black hole formation and the properties of the stablect headings: black hole physics — galaxies: evolution

## M-sigma relation



also Gebhart et al '00

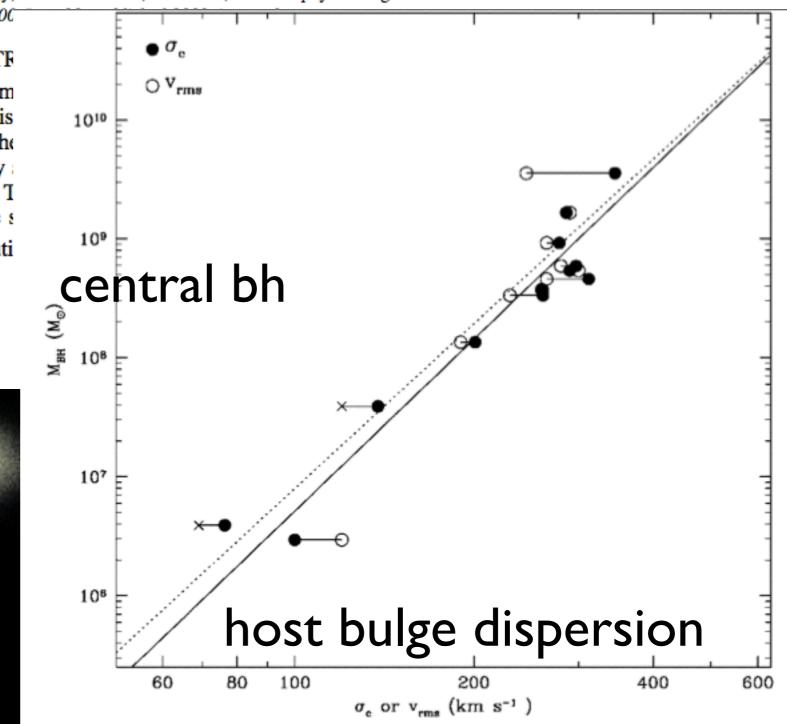
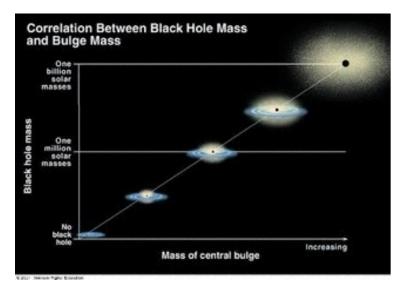


Fig. 2.—BH mass vs. the central velocity dispersion  $\sigma_c$  of the host elliptical galaxy or bulge (filled circles) or the rms velocity  $v_{\rm rms}$  measured at one-fourth of the effective radius (open circles). Crosses represent lower limits in  $v_{\rm rms}$ . The solid and dashed lines are the best linear fits using  $\sigma_c$  (as in Fig. 1b) and



Why surprising?

```
MW:
```

 $M_{BH} \sim 4 \times 10^6 M_{sun}$ 

 $R_{sch} \sim Ikm (M_{BH}/M_{sun})$ 

 $\sim 4 \times 10^6 \text{ km}$ 

 $R_{influence} \sim 1 pc \sim 10^{13} km$ 

 $M_{\text{bulge}} \sim 4 \times 10^9 M_{\text{sun}}$ 

 $R_{\text{bulge}} \sim I \text{kpc} \sim 10^{16} \text{km}$ 

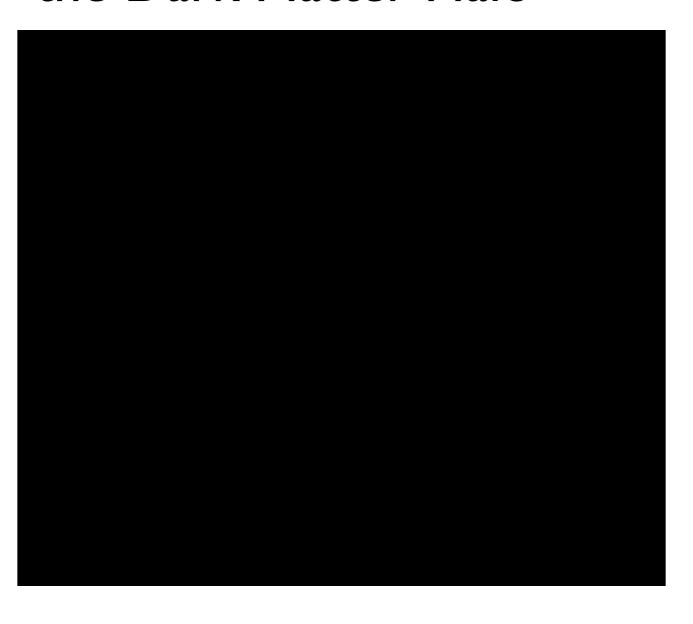
why care?

galaxy and central bh assembled in sync

if understand bh, then galaxy?

gas rich merger vs. dry mergers

## the Dark Matter Halo



- rotation curves
- •numerical simulations
- •gravitational lensing
- dark matter annihilation

## THE STRUCTURE OF COLD DARK MATTER HALOS

Julio F. Navarro<sup>1</sup>

Steward Observatory, The University of Arizona, Tucson, AZ 85721

#### CARLOS S. FRENK

Physics Department, University of Durham, Durham DH1 3LE, England

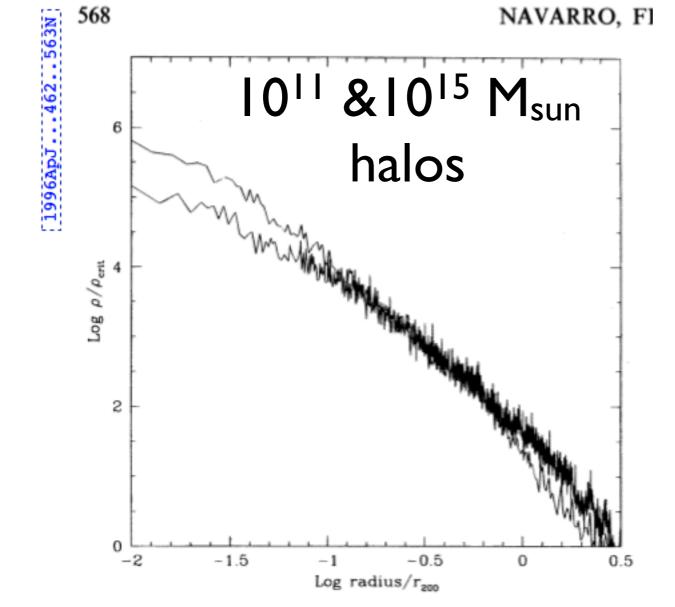
AND

#### SIMON D. M. WHITE

Max-Planck-Institut für Astrophysik, Karl-Schwarzschild Strasse 1, D-85740, Garching, Germany
Received 1995 August 1; accepted 1995 December 4

#### ABSTRACT

We use N-body simulations to investigate the structure of dark halos in the standard cold dark matter cosmogony. Halos are excised from simulations of cosmologically representative regions and are



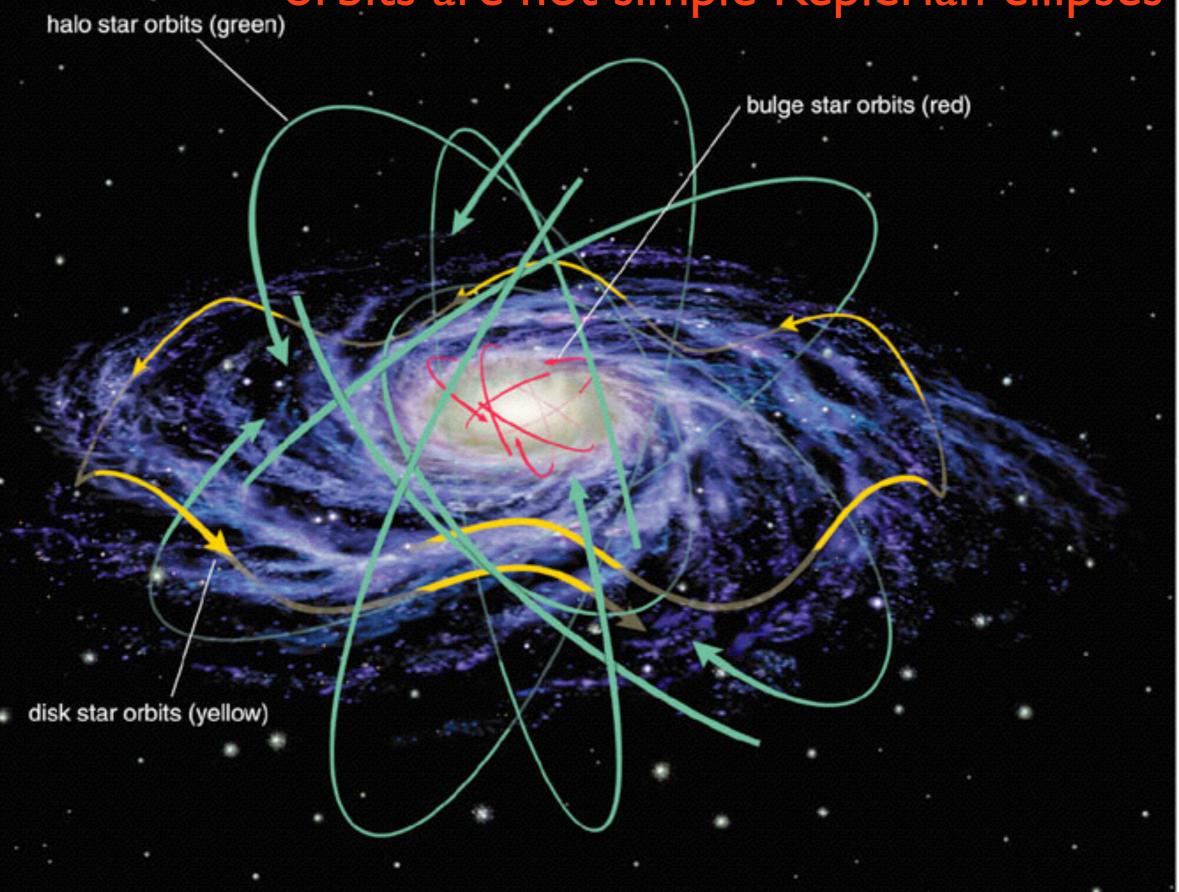
$$\rho(r) = \frac{\rho_0}{(r/a)(1+r/a)^2}$$

gravitational collapse (in an expanding universe) gives an in-explicable universal profile

# Conclusions: multiple components in the MW, assembly history

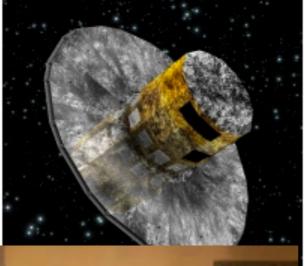
- geometry of MW (thin/thick disks+bulge+halo, the distribution of star light)
- dark matter dominates at large distances (rotation curve)
- the local group (distance to LMC, SMC, dwarf galaxies, missing satellites)
- globular clusters (double MS, mass segregation)
- galactic center (BH, stellar cluster),

# orbits are not simple Keplerian ellipses



## Why is galactic dynamics interesting now?

Gaia is an ambitious mission to chart a three-dimensional map of our Galaxy, the Milky Way, in the process revealing the composition, formation and evolution of the Galaxy. Gaia will provide unprecedented positional and radial velocity measurements with the accuracies needed to produce a stereoscopic and kinematic census of about one billion stars in our Galaxy and



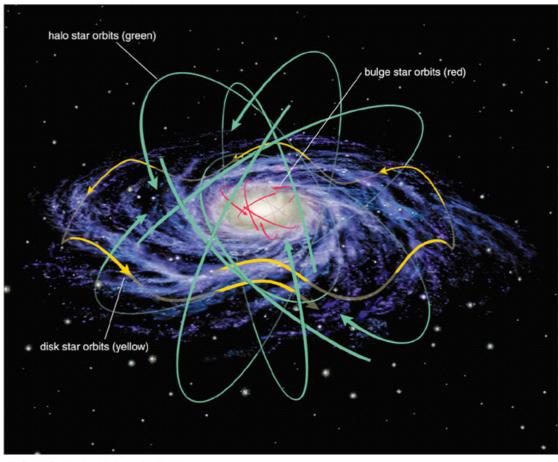


- measure the positions of ~1 billion stars both in our Galaxy and other members of the Local Group, with an accuracy down to 20 µas
- perform spectral and photometric measurements of all objects
- derive space velocities of the Galaxy's constituent stars using the stellar distances and motions
- create a three-dimensional structural map of the Galaxy

The gathered large datasets will provide astronomers with a wealth of information covering a wide range of research fields: from solar system studies, galactic astronomy, cosmology to general relativity.

## ESA's GAIA mission

Launched Dec. 19, 2013 reached L2 point: Jan 8, 2014



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