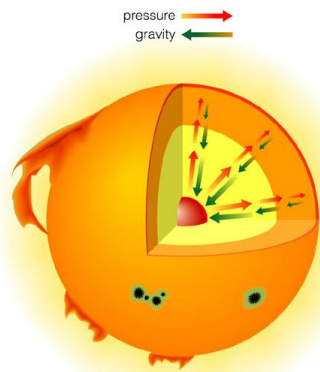


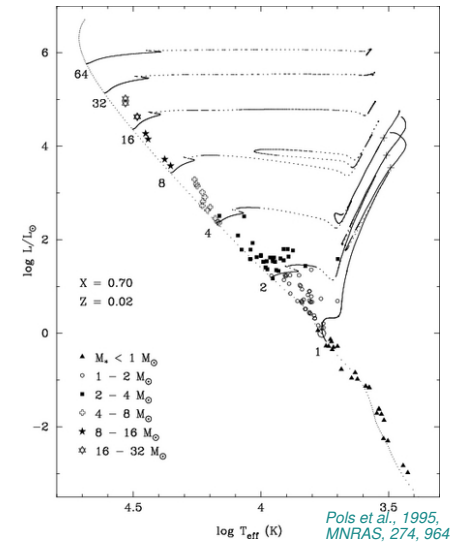
# Star's life: Protracted battle with gravity



- ALWAYS** ⇒ To support weight: need high pressure
- MOSTLY** ⇒ need high temperature
- ⇒ will lose energy
- ⇒ need energy source:
  - Gravitational contraction
  - Nuclear fusion

Ultimately, *Can something else than thermal pressure balance gravity?*

**Evolutionary tracks:**  
what happens depends on mass



- Distance  $d [\text{pc}] = 1/\pi [\text{arcsec}]$
- magnitudes  $m = C - 2.5 \log f; m_1 - m_2 = -2.5 \log (f_1/f_2); M - m = 5 - 5 \log d$
- Doppler shift  $\frac{\Delta \lambda}{\lambda} = \frac{v_{\text{rad}}}{c}$
- Gravity & tides  $a = \frac{GM}{r^2}; a_{\text{tide}} \approx \frac{GM 2R}{r^3}$
- Kepler  $GM = \Omega^2 a^3 = \left(\frac{2\pi}{P}\right)^2 a^3; \frac{a_1}{a} = \frac{v_1}{v} = \frac{m_2}{M};$  for circular orbit,  $v = \sqrt{\frac{GM}{a}}$
- Virial Theorem  $E_{\text{kin}} = -\frac{1}{2} E_{\text{pot}}; E_{\text{rot}} = E_{\text{kin}} + E_{\text{pot}} = \frac{1}{2} E_{\text{pot}};$  [where  $E_{\text{pot, bin}} = -\frac{GM_1 M_2}{a}$  and  $E_{\text{pot, star}} \approx -\frac{GM^2}{R}$ ]
- Ideal gas  $P = nkT = \frac{\rho}{\mu m_H} kT;$  typical kin. en. per particle  $\langle e \rangle = \frac{3}{2} kT;$  en. density  $e = \frac{3}{2} nkT = \frac{2}{3} P$
- Degenerate gas  $\Delta x \Delta p \sim \hbar; E_F = \frac{1}{2} \frac{p_F^2}{m_e} \propto n_e^{2/3}; P \propto n_e E_F \propto n_e^{5/3} \propto (\rho/\mu)^{5/3} \rightarrow R \propto M^{-1/3}$
- Photon propagation  $l_{\text{mp}} = 1/\sigma n = 1/\kappa \rho; t_{\text{random}} = \frac{R}{l_{\text{mp}}} \frac{R}{c}$
- Black body  $L = 4\pi R^2 \sigma T_{\text{eff}}^4; \lambda_{\text{peak}} \propto 1/T$
- Hydrostatic eq.  $\frac{dP}{dr} = -\rho \frac{GM}{r^2}; \rightarrow P \propto M^2/R^4$
- Radiative transfer  $\frac{dT}{dr} = \frac{3\kappa \rho}{16\sigma T^3} \frac{L_r}{4\pi r^2}; \rightarrow L \propto T_c^4 R^2 \frac{l_{\text{mp}}}{R}$
- Timescales  $\tau_g \sim \sqrt{\frac{r^3}{GM}} \sim \sqrt{\frac{1}{G\rho}}; \tau_{\text{KH}} \sim \frac{GM^2/R}{L}$
- Hydrogen fusion  $E = mc^2; p-p$  start with  $p+p \rightarrow D + e^+ + \nu_e;$   
CNO catalyst, start with  $^{12}\text{C} + p \rightarrow ^{13}\text{N} + \gamma$
- Hydrogen atom  $E_n = -13.6 \text{ eV} / n^2$